

$$\partial_t(\sqrt{-g}B^i)=\partial_j(\sqrt{-g}(B^iv^j-B_jv^i))$$